

Part 1

1. The series that $\exp(-x)$ equals
 - a. $1 + x + x^2/2! + \dots$
 - b. $1 - x + x^2/2! - \dots$
 - c. $x - x^3/3! + x^5/5! - \dots$
 - d. $1 - x^2/2! + x^4/4! - \dots$
2. If two rows in a 3×3 matrix are interchanged, the determinant
 - a. remains the same
 - b. changes sign
 - c. becomes zero
 - d. becomes unity
3. The solution of the differential equation $9y \frac{dy}{dx} + 4x = 0$ is (where c is a constant)
 - a. $(x^2/9) + (y^2/4) = c$
 - b. $y = c \exp(4x/9)$
 - c. $y = \cos(x)$
 - d. $y = \sin(x)$
4. Let \mathbf{x} be the vector cross product. Which of the following properties is NOT TRUE?
 - a. $\mathbf{a} \times (\mathbf{b} + \mathbf{c}) = \mathbf{a} \times \mathbf{b} + \mathbf{a} \times \mathbf{c}$
 - b. $(\mathbf{a} + \mathbf{b}) \times \mathbf{c} = \mathbf{a} \times \mathbf{c} + \mathbf{b} \times \mathbf{c}$
 - c. $\mathbf{a} \times \mathbf{b} = -(\mathbf{b} \times \mathbf{a})$
 - d. $(\mathbf{a} \times \mathbf{b}) \times \mathbf{c} = \mathbf{a} \times (\mathbf{b} \times \mathbf{c})$
5. Let u be the displacement of a vibrating elastic string, say, a violin string; let t be the time and x be the position; c is a constant. One can show that such a string is governed by the following partial differential equation:

$$\frac{\partial u}{\partial t} = c \frac{\partial^2 u}{\partial x^2}$$

a.

$$\frac{\partial u}{\partial x} = c \frac{\partial^2 u}{\partial t^2}$$

b.

$$\frac{\partial^2 u}{\partial t^2} = c \frac{\partial^2 u}{\partial x^2}$$

c.

$$\frac{\partial u}{\partial t} = c \frac{\partial u}{\partial x}$$

d.

6. A box contains 10 pens, three of which are defective. Two pens are drawn at random (without replacement – that is, first one pen is drawn and from the remaining 9 pens, another is drawn). What is the probability that both are defective?
- 1/15
 - 1/10
 - 7/15
 - 49/100
7. The square of the standard deviation is the
- Mean
 - Outlier
 - Variance
 - Median
8. The number of ways in which two (indistinguishable) red balls and two (indistinguishable) blue balls can be arranged at the corners of a square is
- 24
 - 4
 - 6
 - 12
9. The eigenvalues of real symmetric matrices are
- pure imaginary
 - pure imaginary or zero
 - real
 - complex
10. Fixed point iteration is an iterative method
- for solving $f(x) = 0$
 - for numerical integration
 - for numerical differentiation
 - for extrapolation of data